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Broadband Coherent Perfect Absorption in Chiral Photonic Systems

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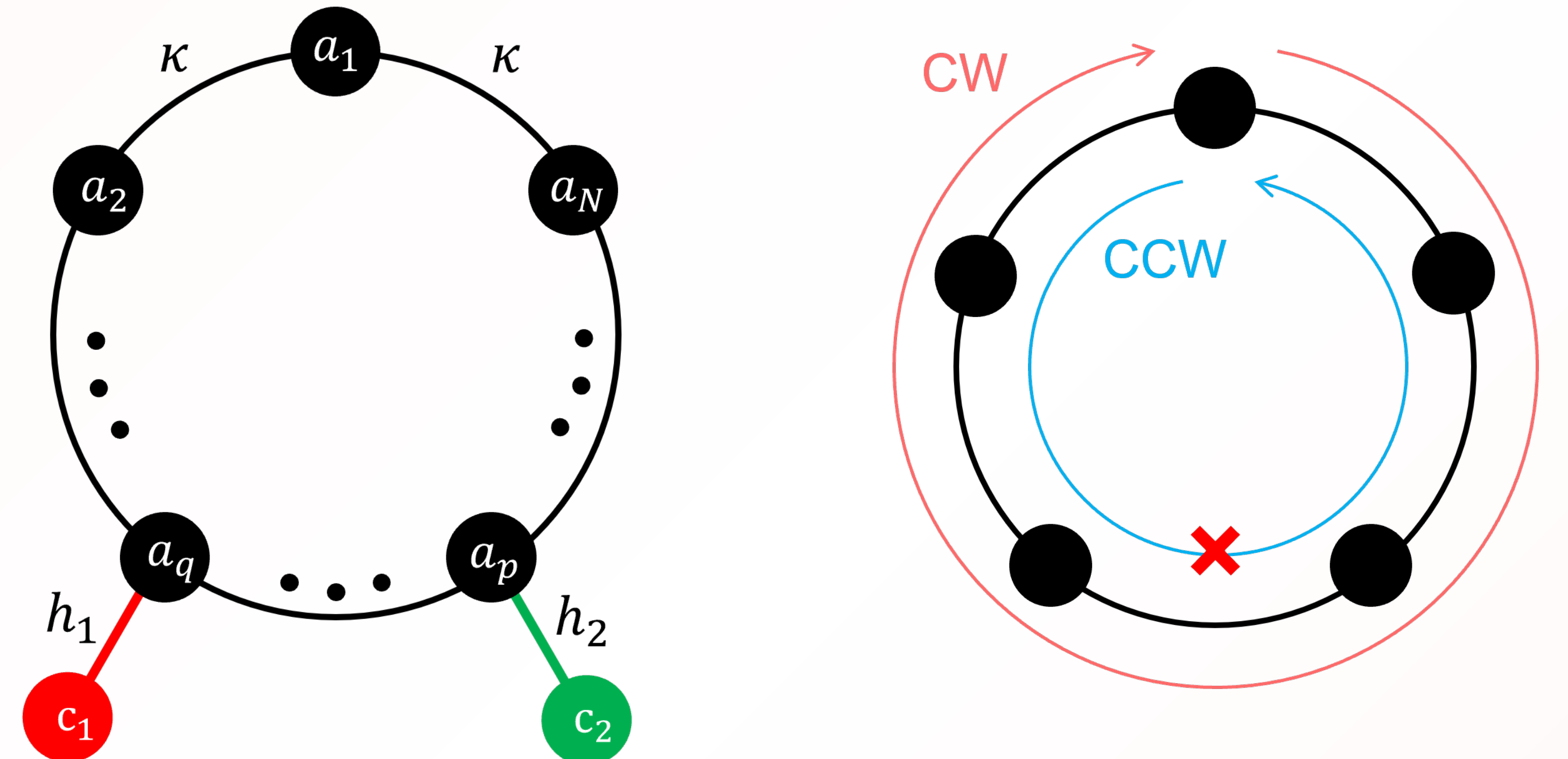
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Introduction

Coherent perfect absorption (CPA) is a steady-state process in which a lossy cavity completely absorbs the energy from an incident wavefront. The phenomenon can be understood as a time reversed lasing: rather than gain induced emission in the absence of driving, CPA results from loss induced destructive interference. Such a delicate process is often assumed to only be achievable for a particular wavefront operating at a specific frequency. Despite this obstacle, it has recently been demonstrated that a broadened CPA linewidth is possible in chiral exceptional point (CEP) systems. In systems where chirality of modes can be established, such as in a microring resonator, operating in the vicinity of an EP induces a chiral wave propagation with handedness associated with the coalescing eigenstates. At the exceptional point, the chirality is reversed, and the wave propagates unidirectionally with handedness given by the Jordan vector, which is opposite to that of the degenerate eigenstate.

To realize a chiral coherent perfect absorption, we use a 1-port discrete photonic ring array with two additional lossy scatterers, where we balance the resonant frequency and loss of these scatterers such that the system operates at an EP. The lossy sites serve to modulate destructive interference, inducing a unidirectional coupling between the propagating and counter-propagating modes of the ring, hence providing a platform to realize a broadband CPA-CEP.

Chirality in a Discrete Photonic Ring Array



Coupled Mode Theory (CMT) System Description:

$$\begin{cases} i \frac{da_n}{dt} = \omega_0 a_n + \kappa a_{n-1} + \kappa a_{n+1} + \delta_{n,p} h_1 c_1 + \delta_{n,q} h_2 c_2 \\ i \frac{dc_1}{dt} = \Omega_1 c_1 + h_1 a_p \\ i \frac{dc_2}{dt} = \Omega_2 c_2 + h_2 a_q \end{cases}; \quad \begin{aligned} k_m &= \frac{2m\pi}{N} \\ \mu_m &= \omega_0 + 2\kappa \cos(k_m) \end{aligned}$$

Mode Space System Description:

$$\begin{cases} i \frac{dA_m}{dt} = \mu_m A_m + \left[\frac{h_1^2}{N\Delta_1} + \frac{h_2^2}{N\Delta_2} \right] A_m + \left[\frac{h_1^2}{N\Delta_1} e^{-2ik_m p} + \frac{h_2^2}{N\Delta_2} e^{-2ik_m q} \right] A_{m'} \\ i \frac{dA_{m'}}{dt} = \mu_{m'} A_{m'} + \left[\frac{h_1^2}{N\Delta_1} + \frac{h_2^2}{N\Delta_2} \right] A_{m'} + \left[\frac{h_1^2}{N\Delta_1} e^{2ik_m p} + \frac{h_2^2}{N\Delta_2} e^{2ik_m q} \right] A_m \\ i \frac{dA_\eta}{dt} = \mu_\eta A_\eta + \left[\frac{h_1^2}{N\Delta_1} + \frac{h_2^2}{N\Delta_2} \right] A_\eta \end{cases}; \quad \begin{aligned} h_j^2 &\ll \Delta_j \ll 1 \\ \eta &\in \left\{ 0, \frac{N}{2} \right\}, \quad m, m' \neq \eta \end{aligned}$$

Chirality Conditions:

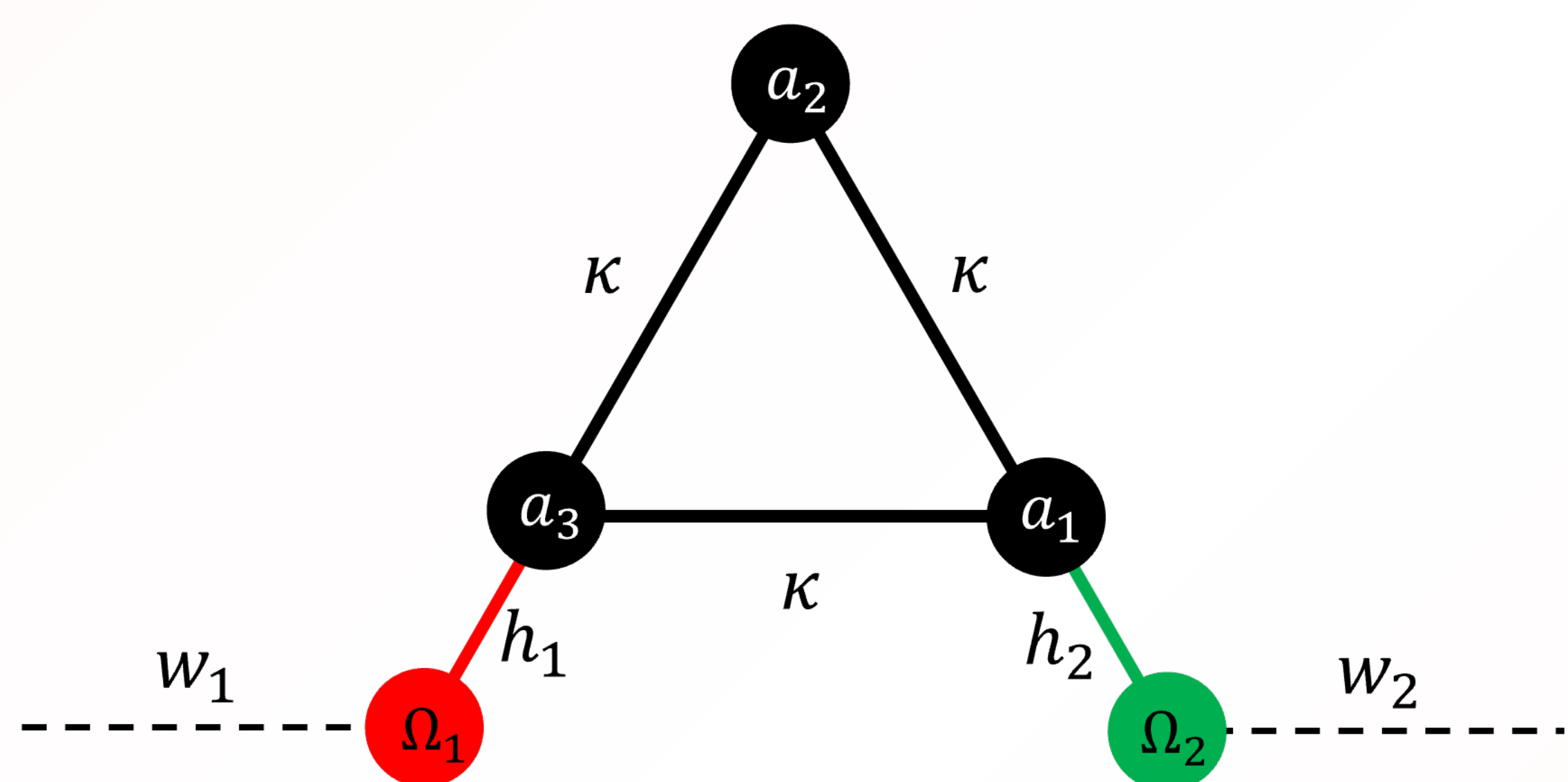
$$\frac{h_j^2}{N\Delta_j} \equiv \chi e^{i\phi_j}, \quad \Delta\phi = \phi_2 - \phi_1$$

Suboptimal Unidirectionality: $N \neq 1, 2, 4$; $\theta \notin \mathbb{Z}$

$$\begin{cases} \Delta\phi = [b + \theta]\pi \\ \theta = \frac{4m(q-p)}{N} \end{cases}; \quad b \in 2\mathbb{Z} + 1$$

Optimal Unidirectionality: $N \in 8\mathbb{Z}$; $\theta \in \mathbb{Z} + \frac{1}{2}$

Coherent Perfect Absorption



Scattering Matrix:

$$S(k) = -1 + 2i \frac{\sin k}{\kappa_1} W^T \frac{1}{\omega(k) - H_{eff}(k)} W; \quad W = \begin{pmatrix} 0 & 0 \\ 0 & 0 \\ w_1 & 0 \\ 0 & w_2 \end{pmatrix}$$

$$H_{eff}(k) = H - \Lambda(k), \quad \Lambda(k) = \frac{e^{ik}}{\kappa_1} W W^T$$

S-Matrix Zeros:

$$\det[S] = \frac{\det[\omega - H_{eff}(-k)]}{\det[\omega - H_{eff}(k)]} \longrightarrow \det[S] = 0 = \det[\omega - H_{eff}(-k)]$$

Wideband Approximation:

$$S(\omega) = -1 + 2i W^T \frac{1}{\omega - H_{eff}} W; \quad H_{eff} = H - \Lambda, \quad H_{dual} = H + \Lambda, \quad \Lambda = i W W^T$$

$$\det[S] = \frac{\det[\omega - H_{dual}]}{\det[\omega - H_{eff}]} \longrightarrow \det[S] = 0 = \det[\omega - H_{dual}]$$

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1. Yan V Fyodorov, Suwun Suwunnarat, and Tsampikos Kottos. Distribution of zeros of the S-matrix of chaotic cavities with localized losses and coherent perfect absorption: non-perturbative results. *Journal of Physics A: Mathematical and Theoretical*, 50(30):30LT01, Jun 2017.
2. A. Hashemi, S. M. Rezaei, S. K. Ozdemir, and R. El-Ganainy. New perspective on chiral exceptional points with application to discrete photonics. *APL Photonics*, 6(4):040803, Apr 2021.
3. S. Soleymani, Q. Zhong, M. Mokim, S. Rotter, R. El-Ganainy, and S. K. Ozdemir. Chiral coherent perfect absorption on exceptional surfaces, 2021.
4. William R. Sweeney, Chia Wei Hsu, Stefan Rotter, and A. Douglas Stone. Perfectly absorbing exceptional points and chiral absorbers. *Physical Review Letters*, 122(9), Mar 2019.

